JOURNAL

OF THE AMERICAN CHEMICAL SOCIETY

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VOLUME 92, NUMBER 13 JULY 1, 1970

Physical and Inorganic Chemistry

Studies of Polyatomic Molecules Using Self-Consistent-Field Wave Functions. B_4H_{10} , B_5H_9 , and B_5H_{11}

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Abstract: SCF wave functions for B_4H_{10} , B_5H_9 , and B_5H_{11} show (1) all atomic (Mulliken) charges are less than ± 0.1 e, (2) apex borons are more negative than other borons, (3) borons in BH₂ groups are more positive than borons in BH groups, (4) no simple correlation exists between one-center diagonal F-matrix elements and charge, (5) all terminal hydrogens are negative and all bridge hydrogens are positive, (6) most properties of the unique hydrogen in the symmetry plane of B_5H_{11} are intermediate between bridge and terminal hydrogens, (7) bridge hydrogens between BH and BH₂ groups are more strongly bonded toward the BH group, and (8) very low electron density directly between two B atoms exists if these borons are joined by a bridge hydrogen.

For some 40 years the ideas underlying the chemistry of electron-deficient molecules have been a challenge to theoretical and experimental chemists.¹⁻⁵ The boron hydrides, based upon polyhedra or their fragments, display an extensive chemistry. Both the geometrical and valence structures have correlated² much of the chemistry, and have provided impetus for discoveries of new species and reactions.

Wave functions based upon the extended Hückel (EH) method, which was developed, formalized, and programmed first⁶ for the boron hydrides, have been given a logical foundation and improvement by parametrization from self-consistent-field (SCF) model calculations.⁷ A next more sophisticated step is the evaluation of accurate SCF wave functions for these boron hydrides. Owing to our desire for transferable parameters among atoms in molecules, as well as for extension of the SCF method to complex molecules, we employ Slater-type orbitals within a minimum basis set.

An accurate SCF wave function and localized valence structure have been reported recently⁸ for B₂H₆. Strong support for a localized bridge threecenter BHB bond was obtained, and boron hybrids of sp^{2.5} were obtained from the optimized minimum basis set. In the present study we extend these SCF calculations and analysis of the wave functions to B_4H_{10} , B_5H_9 , and B_5H_{11} .

In undertaking these SCF computations we have hoped to provide a quantitative basis for correlating some of the fascinating experimental observations on boron hydrides. Although our ab initio LCAO SCF calculations are among the most accurate which have been performed on larger molecules, we have tried to restrict our discussions only to those molecular properties where we can hope to obtain relatively unambiguous and physically relevant interpretations despite the limitations of the SCF approximations. The wave functions we present in this paper are the basis for

⁽¹⁾ K. Freudenberg, "Intramolekulare Umlagerung Optischaktiver Systeme," from the Sitzungberichte der Heidelberger Akademie der Wissenschaften, Walter de Gruyter and Co., Berlin and Leipzig, 1927.
(2) W. N. Lipscomb, "Boron Hydrides," W. A. Benjamin, Inc., New York, N. Y. 1963.

^{(3) (}a) J. O. Hirschfelder, H. Eyring, and N. Rosen, J. Chem. Phys.,
4, 130 (1936); (b) J. O. Hirschfelder, *ibid.*, 6, 795 (1938).
(4) H. C. Longuet-Higgins, J. Chim. Phys., 46, 269 (1949).
(5) S. Winstein and H. J. Lucas, J. Amer. Chem. Soc., 60, 836 (1938).

⁽⁶⁾ R. Hoffmann and W. N. Lipscomb, J. Chem. Phys., 36, 2179 (1962).

⁽⁷⁾ F. P. Boer, M. D. Newton, and W. N. Lipscomb, J. Amer. Chem. Soc., 88, 2361 (1966).

⁽⁸⁾ E. Switkes, R. M. Stevens, W. N. Lipscomb, and M. D. Newton, J. Chem. Phys., 51, 2085 (1969).



Figure 1. B₄H₁₀.





studies of three such properties which may be analyzed in terms of the one-electron charge distribution.

A primary aim of our calculations has been to provide an ab initio analysis of bonding in the polyhedral boron hydrides. In this paper we discuss the interpretation of previously proposed bonding schemes in terms of the calculated electron densities, net atomic charges, and overlap populations. In the following paper⁹ we include a detailed analysis of bonding, preferred valence structures, and equivalent resonance structures in terms of localized orbital transformations on the SCF wave functions for B_4H_{10} , B_5H_9 , and B_5H_{11} . Another aim of these calculations has been to relate wave functions to magnetic properties and chemical reactivities of boron hydrides. We discuss below possible relations of the calculated ground-state charge densities to these properties. Presently one of the authors (J. A. T.) is applying the SCF wave functions to somewhat more detailed calculations of the ¹H and ¹¹B chemical shifts in these molecules. By utilizing the available wave functions for this series of four related molecules $(B_2H_6, B_4H_{10}, B_5H_9, \text{ and } B_5H_{11})$, we may obtain interpretations of the trends in boron-11 chemical shifts among nuclei in different molecules as well as look at the relative shifts of boron nuclei in different geometric positions of the same molecule. This forthcoming analysis will be especially interesting because of the paramagnetic susceptibility predicted by a very complete coupled Hartree-Fock calculation¹⁰ for



(10) (a) R. M. Stevens and W. N. Lipscomb, J. Chem. Phys., 42, 3666 (1965); (b) R. A. Hegstrom and W. N. Lipscomb, *ibid.*, 45, 2378 (1966).



Figure 3. B₅H₁₁.

the closed-shell ${}^{1}\Sigma$ state of diatomic BH. We also present a very qualitative discussion of reactivities in these boron hydrides. More quantitative calculations, now in progress, will be the topic of a subsequent publication. The level of reliability of these SCF wave functions for a series of related molecules may permit correlation of the relative reactivities for borons in different hydrides as well as explain the differences in reactivity for borons at nonequivalent sites in the same molecule, in those reactions in which the transition state retains some features of the initial charge distribution.

As large polyatomic calculations using Slater-type orbitals become feasible one may compare the results with those of other *ab initio* and empirical methods and reevaluate the strengths and limitations of the SCF approximation. For this purpose we report the SCF energies, dipole moments, Koopmans ionization potentials, atomic populations, and atomization energies calculated from our wave functions. Using an approximate, but nonempirical, method, Boer, Newton, and Lipscomb^{7,11} have studied these boron hydrides. We discuss their predictions on the transferability of diagonal SCF one-electron Hamiltonian elements and their other approximations. We compare our results with those obtained by their method as well as with those from semiempirical calculations.

Calculations

Our LCAO SCF calculations were performed on an IBM 7094, Model I, computer using a modified version of the program described by Stevens.¹² The geometries of the boron frameworks have been taken from X-ray diffraction studies¹³⁻¹⁵ and the hydrogen coordinates have been idealized using suggested angles and distances.² The assumed symmetries were C_{2v} , C_{4v} , and C_s for B_4H_{10} , B_5H_9 , and B_5H_{11} , respectively. The coordinates of the unique atoms are given in Table I. Our labeling of the atoms is shown in Figures 1–3.

Our basis consisted of a minimum set of Slater-type orbitals with exponents taken from an optimized calculation for diborane.⁸ These exponents are 1.147

(11) F. P. Boer, "Molecular and Valence Structures of Boron Compounds," Ph.D. Thesis, Harvard University, 1965.

(12) R. M. Stevens, J. Chem. Phys., 52, 1397 (1970).

(13) C. E. Nordman and W. N. Lipscomb, *ibid.*, 21, 1856 (1953), B₁H₁₀ structure.
(14) W. J. Dulmage and W. N. Lipscomb, Acta Crystallogr., 5, 260

(14) W. J. Duimage and W. N. Lipscomb, Acta Crystallogr., 5, 200 (1952), B₅H₉ structure.

(15) L. R. Lavine and W. N. Lipscomb, J. Chem. Phys., 22, 614 (1954), B₅H₁₁ structure.

Table I. Unique Coordinates for Boron Hydrides (au)

		x	У	z
$B_4 H_{10^a}$ 1	Ht	2.71313	0.0	-1.98557
3	BH ^t	0.0	2.67363	3.82733
5	5Ht	0.0	4.42724	0.22396
1	H _b	2.57295	1.81222	1.4 79 06
1	B	1.65354	0.0	0.0
3	3 B	0.0	2.63244	1.57889
B₅H₅ ^b 1	H_t	0.0	0.0	4.30542
2	$2H_t$	4.42977	0.0	0.91555
1	lH⊾	1.84496	1.84496	-1.68509
1	B	0.0	0.0	2.05662
2	2B	2.36580	0.0	0.0
B ₅H ₁₁ ° 1	lHt	0.0	1.99750	3. 99 470
2	$2H_t$	0.0	4.19050	0.77060
3	$3H_t$	2.78980 -	-1.64580	1.04810
5	$5H_t$	4.70746	3.28840	1.3345
7	$7H_t$	2.48090	4.68300	-1.50250
1	lH _b	0.0 -	-0.30120	-1.87730
2	2H _b	2.72120	1.35970	-1.86100
1	B	0.0	2.16740	1.75240
2	2B	1.67240	0.0	0.0
۷	4B	2.91140	3.0063	0.0

^a xz and yz are symmetry planes. ^b z is a symmetry axis. ^c yz is the symmetry plane.

Energetics

The total energies and virial ratios from our wave functions are given in Tables II, III, and IV. Deviations of the virial ratio from unity are small and comparable in magnitude to that for $B_2H_{6.8}$ Slightly larger deviations in the higher hydrides are expected because of the greater uncertainties in the molecular geometry and lack of reoptimization of exponents.

In Table V we compare the atomization energies calculated from our wave functions with values from more approximate calculations and from experiment. The accurate estimation of reaction energies from Hartree-Fock wave functions requires either a consistent cancellation of correlation energies or an appropriate estimate of these quantities. We suggest that minimum basis set calculations such as ours do not treat molecules with an accuracy comparable to an optimized single-⁷ atomic calculation,¹⁷ and thus we present both the usual atomization energies utilizing Clementi's atomic energies¹⁷ and atomization energies utilizing SCF calculations for boron and hydrogen,

Table II. B₄H₁₀ Occupied (and Lowest Unoccupied) Molecular Orbitals and Energies

		-7.6174	-7.6174	-7.5979	-7.5976	-0.9455	-0.7727	-0.7441	-0.6291	-0.5579	-0.5534	-0.5141	-0.5033	-0.4898	-0.4544	-0.4312	0.2435
1 H7	15	0.000	0.000	0.003	0.003	0.054	0.000	-0.121	0.225	0.000	-0.111	0.000	0.281	0.421	0.000	0.081	0.000
2 H 7	15	0.000	0.000	0.003	-0.003	0.054	0.000	0.121	0.225	0.000	-0.111	0.000	0.281	-0.421	0.000	0.081	0.000
3 H 7	15	0.004	0.004	0.000	0.000	0.058	0.139	0.000	-0.252	0.000	-0.027	0.374	0.215	0.000	-0.136	0.267	0.267
4 H 7	15	-0.004	0.004	0.000	C.000	0.058	-0.139	0.000	-0.252	0.000	-0.027	-0.374	0.215	0.000	0.136	0.247	-0.257
5H7	15	0.003	0.004	0.000	0.000	0.048	0.145	0.000	-0.067	0.000	-0.363	-0.216	-0.157	0.000	-0.353	-0.042	0.071
6H7	15	-0.003	0.004	0.000	0.000	0.048	-0.145	0.000	-0.067	0.000	-0.363	0.216	-0.157	0.000	0.353	-0.042	-0.021
1 H 8	15	0.002	0.002	0.003	0.003	0.124	0.157	-0.226	-0.039	-0.306	0.040	-0.013	0.073	-0.135	0.144	-0.256	-0.548
2 H B	15	0.002	0.002	0.003	-0.003	0.124	0.157	0.226	-0.039	0.306	0.040	-0.013	0.073	0.115	0.188	-0.256	-0.548
3H8	15	-0.002	0.002	0.003	-0.003	0.124	-0.157	0.226	-0.039	-0.306	0.040	0.013	0.073	0.135	-0.188	-0.256	0.548
4 H B	15	-0.002	0.002	0.003	0.003	C.124	-0.157	-0.226	-0.039	0.306	0.040	0.013	0.073	-0.135	-0.188	-0.256	0.548
18	15	0.000	-0.005	-0.703	-0.703	-0.122	0.000	0.116	-0.090	0.000	-0.023	0.000	-0.012	-0.050	c.000	-0.015	0.000
	25	0.000	0.003	-0.018	-0.023	0.257	0.000	-0.307	0.260	0.000	0.073	0.000	0.035	0.140	C.000	0.046	0.000
	2 P 2	0.000	0.001	-0.002	-0.001	0.077	0.000	-0.076	-0.151	0.000	0.165	0.000	-0.151	-0.302	0.000	-0.195	6.00
	2 P X	0.000	-0.002	-0.001	0.003	-0.077	0.000	-0.091	-0.037	0.000	-0.091	0.000	C.287	0.104	0.000	-0.334	0.000
	2 P Y	0.003	0.000	0.000	0.000	0.000	0.152	0.000	0.000	-0.238	0.000	-0.097	0.000	0.000	0.231	0.000	0.221
28	15	0.000	-0.005	-0.703	0.703	-0.122	0.000	-0.116	-0.090	0.000	-0.023	0.000	-0.C1Z	0.050	0.000	-0.015	C.COO
	25	0.000	0.003	-0.018	0.023	0.257	0.000	0.307	0.260	0.000	0.073	0.000	0.035	-0.140	c.000	0.046	0.000
	2 P 2	0.000	0.001	-0.002	0.001	0.077	0.000	0.076	-0.151	0.000	0.165	0.000	-0.151	0.302	0.000	-0.195	C.000
	ZPX	0.000	0.002	0.001	0.003	0.077	0.000	-0.091	0.037	0.000	0.091	0.000	-0.287	0.134	c.00C	0.334	0.000
	ZPY	0.003	0.000	0.000	0.000	0.000	0.152	0.000	0.000	0.238	0.000	-0.097	0.000	0.000	0.231	0.000	0.221
3 B	15	-0.703	-0.703	0.005	0.000	-0.100	-0.139	0.000	0.073	0.000	0.058	-0.016	0.021	0.002	0.029	-0.032	-0.058
	25	-0.020	-0.020	0.004	0.000	0.207	0.350	0.000	-0.205	0.000	-0.172	0.047	-0.062	0.000	-0.081	0.102	0.262
	ZPZ	0.001	0.001	-0.002	0.000	-0.027	-0.017	0.000	-0.167	0.000	0.114	0.352	0.239	0.000	-0.028	0.136	-0.221
	298	0.000	0.000	0.000	0.001	0.000	0.000	-0.146	0.000	-0.256	0.000	0.000	0.000	-0.121	0.000	C.000	0.000
	ZPY	0.002	0.002	-0.003	0.000	-0.078	-0.022	0.000	-0.042	0.000	-0.268	-0.072	0.010	0.000	-0.317	-0.048	-0.361
• 5	15	0.703	-0.103	0.005	0.000	-0.100	0.139	0.000	0.073	0.000	0.058	0.016	0.021	0.000	-0.029	-0.032	0.058
	23	0.020	-0.020	0.004	0.000	0.207	-0.350	0.000	-0.205	0.000	-0.172	-0.047	-0.062	c.con	0.081	0.102	-0.262
	242	-0.001	0.001	-0.002	0.000	-0.027	0.017	0.000	-0.167	0.000	0.114	-0.352	0.239	0.000	0.028	0.136	0.221
	244	0.000	- 0 00 7	0.000	0.001	0.000	-0.000	-0.140	0.000	0.256	0.000	0.000	0.000	-C.121	0.000	0.000	C.COO
	281	0.002	-0.002	0.003	0.000	0.078	-0.022	0.000	0.042	0.000	0.268	-0.072	-0.010	0.000	-0.317	0.048	-0.361
	Electr Nucle	onic energy ar repulsion	• -208.140 • 103.884)3 au 14 au	Two-elec Kir	tron energ netic energ	ry • 134.08 ry • 104.25	89 au 16 au									
		lotal energy	• -104. 255	9 au		-E/	⊺• 1.00	004									

for terminal hydrogens, 1.209 for bridge hydrogens, 4.680 for boron 1s, 1.443 for boron 2s, and 1.477 for boron 2p. Each unique integral over atomic orbitals was calculated to at least five decimal place accuracy. and full advantage was taken of molecular symmetry. Approximate computation times were 116, 140, and 320 min for B_4H_{10} , B_5H_9 , and B_5H_{11} , respectively.

The wave functions and SCF energies are listed in Tables II, III, and IV. Although our calculations employ minimum basis sets, their quality is enhanced by the favorable ratio of basis functions to electron pairs in minimum basis sets for neutral boron hydride molecules. This 2:1 ratio provides a freedom not available in minimum basis set calculations involving heavier atoms of the first row in the periodic table, and is shown in B_2H_{δ} by the relatively small energy improvement found by extending the basis set.^{8,16} However, extension of the basis set may allow for adequate polarization at the H atom positions.

(16) R. T. Buenker, S. D. Peyerimhoff, L. C. Allen, and J. L. Whitten, J. Chem. Phys., 45, 2835 (1966).

which use our optimized molecular exponents from diborane. The surprising degree of cancellation of energy errors arising from correlation, atomic orbital contraction,¹⁸ and our limited basis sets, evidenced in the latter method for calculating the atomization energies of boron hydrides, is also found in calculations on hydrocarbons.¹⁹ Here atomic energies calculated using optimized molecular exponents were subtracted from the molecular energies. We emphasize the fortuitous, if consistent, nature of such an approximation or "prescription" for atomization energies and refer to more complete discussions which make the correct alterations on experimental enthalpies before comparison with calculated electronic energies.²⁰ Table V also contains the ratios of these atomization energies to the corresponding energies of B_2H_6 . As may be

(17) E. Clementi and D. L. Raimondi, *ibid.*, 38, 2686 (1963).
(18) K. Ruedenberg, *Rev. Mod. Phys.*, 34, 326 (1962).

(19) E. Switkes and J. Tossell, unpublished results.

(20) (a) L. C. Snyder, J. Chem. Phys., 46, 3602 (1967); (b) L. C.
 Snyder and H. Basch, J. Amer. Chem. Soc., 91, 2189 (1969).

Table III. B₅H₉ Occupied (and Lowest Unoccupied) Molecular Orbitals and Energies

		-7.6112	-7.6110	-7.6110	-7.6106	-7.5018	-1.0219	-0.7761	-0.7761	-0.6801	-0.5804	-0.5707	-0.5590	-0.5104	-0.5104	-0.4611	-0.3794	-0.3794	0.1905
181	15	-0.000	0.000	0.000	0.000	-0.004	-0.034	0.000	0.000	-0.172	0.125	0.000	0.000	0.000	0.000	-0.556	0.000	0.000	0.000
2 HT	15	6 .00 Z	0.003	0.000	~0.002	0.000	-0.035	-0.127	0.000	-0.003	0.237	0.000	-0.286	-0.370	0.000	0.120	0.168	C.000	-0.161
3H1	15	0.002	0.000	0.003	0.002	0.000	-0.035	0.000	-0.127	-0.003	0.237	0.000	0.286	0.000	-0.370	0.120	c •000	0.168	0.161
4 H7	15	0.002	-0.003	0.000	-0.002	0.000	-0.035	0.127	0.000	-0.003	0.237	0.000	-0.286	0.370	0.000	0.120	-0.168	0.000	-0.161
5 H 7	15	0.002	0.000	-0.003	0.002	0.000	-0.035	0.000	0.127	-0.003	0.237	0.000	0.286	0.000	0.370	0.120	0.000	-C.168	0.161
THE	15	0.004	0.003	0.003	0.000	0.000	-0.107	-0.192	-0.192	0.205	0.021	0.295	0.000	0.186	0.186	-0.109	0.145	0.145	0.000
2 HE	15	0.004	-0.003	0.003	0.000	0.000	-0.107	0.192	-0.192	0.205	0.021	-0.295	0.000	-0.186	0.186	-0.109	-0.145	0.145	0.000
2 146	15	0.004	-0.003	-0.003	0.000	0.000	-0.107	0.192	0.192	0.205	0.021	0.295	0.000	-0.186	-0.186	-0.109	-0.145	-0.145	0.000
- 116	15	0.004	0.003	-0.003	0.000	0.000	-0.107	-0.192	0.192	0.205	0.021	-0.295	0.000	0.166	-0.186	-0.109	0.145	-0.145	0.000
16	15	-0.006	0.000	c.cco	0.000	0.994	0.105	0.000	0.000	0.159	0.001	0.000	0.000	0.000	0.000	0.073	0.000	0.000	0.000
	25	0.007	0.000	0.000	0.000	0.033	-0.161	0.000	0.000	-0.387	0.026	0.000	0.000	0.000	0.000	-0.212	0.000	0.000	0.000
	272	-0.002	0.000	0.000	0.000	-0.007	4.124	0.000	0.000	0.070	0.173	0.000	0.000	c.000	0.000	-0.409	0.000	c.000	0.000
	201	0.000	0.004	0.000	0.000	0.000	0.000	-0.106	0.000	0.000	0.000	0.000	0.000	-0.087	0.000	0.000	-0.423	C.CC0	0.000
2.	201	-0.497	-0.303	0.004	0.000	0.000	0.000	0.000	-0.106	0.000	0.000	0.000	0.000	0.000	-0.087	0.000	0.000	-0.423	0.000
20		-0.013	-0.031	0.000	0.014	-0.003	0.105	0.140	0.000	-0.003	-0.030	0.000	0.080	0.038	0.000	-0.027	0.024	0.000	-0.058
	207	-0.001	-0.021	0.000	-0.000	-0.003	-0.193	-0.355	0.000	0.016	0.102	0.000	-9.237	-5.104	0.000	0.084	-0.040	C.000	0.313
	20.4	0.001	0.001	0.000	-0.000	-0.003	0.010	0.034	0.000	-0.142	0.048	0.000	-0.035	-0.238	0.000	0.108	-0.304	0.000	-0.510
	20.0	0.000	0.000	0.000	-0.004	0.002	0.000	0.045	0.000	0.003	0.235	0.000	-0.105	-9.247	0.000	0.022	0.323	0.000	0.034
38	16	-0.697	0.000	-0.703	-0.697	-0.003	0.000	0.000	-0.150	-0.000	0.000	0.260	0.000	0.000	0.100	-0.037	0.000	-0.128	0.000
		-0.012	0.060	-0.021	-0.014	-0.005	-0.193	0.000	-0.140	-0.003	-0.030	0.000	-0.000	0.000	-0.036	-0.027	0.000	0.024	0.058
	207	0.001	0.000	0.001	0.000	-0.003	0.010	0.000	-0.019	-0.103	0.102	0.000	0.237	0.000	-0.214	0.104	0.000	-0.040	
	201	0.000	0.002	0.000	0.000	0.000	0.000	-0.150	0.000	-0.172	0.040	0.000	0.035	0.100	0.000	0.000	-0.138	-0.304	0.510
	2.04	0.000	0.000	0.003	0.004	4.002	0.114	-0.156	0.045	0.000	0.000	0.200	0.000	0.100	-0.347	0.000	-0.128	0.000	0.000
48	1 k	-0.457	0.703	0.000	6.497	-0.003	u.105	-0.140	0.000	-0.003	-0.010	0.000	0.105	3.000	0.000	-0.027	-0.034	6.000	-0.024
		-0.012	0.021	0.000	0.014	-0.005	-0.193	-0.140	0.000	-0.005	-0.030	0.000		-0.030	0.000	0.045	-0.024	0.000	-0.03%
	292	0.001	-0.001	0.000	-0.000	-0.003	0.010	-0.019	0.000	-0.192	0.048	0.000	-0.016	0 114	0.000	0.106	0.344	0.000	-0.510
	2 P X	-0.000	0.003	0.000	0.004	-0.002	-0.114	0.045	0.000	-0.061	-0.235	0.000	0.145	-0.247	0.000	-0.022	0.121	0.000	-0.084
	2.04	0.000	0.000	0.002	0.000	0.000	0.000	0.000	-0.158	0.000	0.000	-0.260	0.000	0.000	0.100	0.000	0.000	-0 124	0.000
58	15	-0.497	0.000	0.703	-0.497	-0.003	0.105	0.000	-0.140	-0.003	-0.030	0.000	-0.080	0.000	-0.036	-0.027	0.000	-0.024	0.058
	25	-0.012	0.000	0.021	-0.018	-0.005	-0.193	0.000	0.355	0.016	0.102	0.000	0.237	0.000	0.104	0.065	0.000	0.090	-0.313
	2 P Z	0.001	0.000	-0.001	0.000	-0.003	0.010	0.000	-0.039	-0.192	0.048	0.000	9.635	0.000	0.218	0.106	0.000	0.304	0.510
	2P X	0.000	0.002	0.000	0.000	0.000	0.000	-0.158	0.000	0.000	0.000	-0.260	0.000	0.100	0.000	0.000	-0.128	0.000	0.000
	284	-0.000	0.000	0.003	-0.004	-0.002	-0.114	0.000	0.045	-0.063	-0.235	0.000	-0.165	c .000	-0.247	-0.022	0.000	0.323	0.084
	51aa1a		- 145 03	67 a.u	Ture alor			47											
Liectronic energy * -205, 6557 au IWo-electron energy * 1/5, 5347 au																			
Nuclear repulsion • 137, 5292 au Kinetic energy • 128, 6543 au																			
Total energy - 128 3065 au																			
		iowi energj	120.70				0.7	71.00											
															_				

Table IV. B₅H₁₁ Occupied (and Lowest Unoccupied) Molecular Orbitals and Energies

		-7.6385	-7.6383	-7.6012	-7.6012	-7.5445	-1.0016	-0.8365	-0.7697	-0.6864	-0.6118	-0.5903	-0.5502	-0.5430	-0.5040	-0. 4738	-0.4736	-0.4364	-0.4013	0.1770
LHT	15	0.000	0.000	0.000	-0.000	0.009	-0+035	0.000	-0.070	-0.168	-0.077	0.000	0.000	0.056	0.117	-0.523	0.000	-0.153	0.000	0.000
2 HT	15	0.000	0.000	0.000	0.003	0.005	-0.103	0.000	-0.286	-0.083	0.185	0.000	0.000	-0.226	-0.132	-0.043	0.000	0.343	0.000	0.000
311	15	-0.003	0.003	0.000	-0.000	-0.000	-0.045	0.066	0.077	-0.075	-0.226	0.268	0.176	-0.184	-0.221	0.025	-0.268	0.053	0.025	-0.054
E F	15	-0.003	-0.003	-0.000	-0.000	-0.000	-0.045	-0.066	0.077	-0.075	-0.226	-C.268	-0.176	-0.164	-0+221	0.025	0.268	0.053	-0.025	0.054
381		0.000	-0.000	-0.003	0.003	-0.000	-0.026	0.074	-0.084	0.060	-0.187	-0.155	0.266	-0.047	0.320	0.105	0.082	0.101	-0.247	0.072
27	13	-0.000	0.000	0.003	0.003	-0.000	-0.026	-0.379	-0.064	0.060	-0.187	0.155	-0.286	-0.047	0.320	0.105	-0.082	0.101	0.247	-0.072
	13	-0.000	-0.000	-0.003	0.003	-0.000	-0.036	0.084	-0.100	0.136	0.012	-0.235	-0.036	-0.215	-0.023	0.005	-0.320	-0.331	0.150	-0.079
1 44	12	-0.006	0.000	0.000	-0.000	-0.000	-0.157	-0.089	-0.100	0.130	0.012	0.235	0.036	-0.215	-0.023	0.005	0.320	-0.331	-0.150	0.079
2 14		-0.003	0.001	-0.003	-01000	-0.000	-0.114	0.000	0.350	0.037	0.224	0.000	0.000	-0.231	0+252	-0.154	0.000	0.158	0.000	0.000
1	12	-0.003	-0.003	0.003	0.003	-0.000	-0.116	-0.117	0.044	0.254	-0.063	0.050	-0.233	0.152	-0.107	-0.157	0.025	0.026	-0.230	0.084
1.4	16	0.003	0.000	0.000	-0.001	-0.994	0.107	0.000	0.001	0.234	-0.083	-0.050	0.253	0.152	-0.107	-0.157	-0.025	0.026	0.230	-0.084
	25	-0.005	0.000	0.000	0.004	-0.032	-0.190	0.000	-0.226	-0.114	0.019	0.000	0.000	-0.034	-0.004	0.055	0.000	0.007	0.000	0.000
	201	0.002	0.000	0.000	-0.001	0.005	0.102	0.000	0.050	0.001	-0 110	0.000	0.000	0.114	0.02	-0.180	0.000	-0.017	0.000	0.000
	2.0 %	0.000	0.002	-0.003	0.000	0.000	0.000	0.107	0.000	0.000	-0.130	0.000	0.000	-0.024	0.107	-0.424	0.000	-0.100	0.000	0-000
	2PY	0.003	0.000	0.000	0.001	0.000	0.017	0.000	-0.133	6.065	0.092	0.000	0.000	-0.144		-0.000	0.177	C.000	0.379	0.152
28	15	0.703	-0.703	-0.004	0.003	0.002	0.118	-0.091	-0.077	0.034	0.035	-0.092	-0.015	0.009	0.031	-0.025	0.000	0.348	0.000	0.000
	25	0.019	-0.023	-0.002	0.003	0.004	-0.238	0.223	0.399	-0.093	-0.107	0.276	0.040	-3.030	-0.044	-0.023	- 6 010	0.00	-0.018	-0.043
	2 P Z	-0.001	0.000	-0.000	0.000	0.002	0.027	-0.035	-0.083	-0.162	-0.134	0.033	0.164	0.018	-0.082	0.144	-0.030	-0.011	0.062	0.240
	2 P X	c.000	0.003	-0.001	0.001	-0.001	0.073	0.065	-0.086	0.124	-0.201	C.107	0.029	0.043	-0.199	-0.099	-0.014	-0.151	0.197	-0.527
	2PV	0.003	-0.002	-0.002	0.002	0.002	-0,688	0.099	-0.072	0.038	0.085	-0.090	-0.109	0.290	0.054	0.069	0.754	-0.011	-0.072	-0.082
38	15	0.703	0.703	0.004	0.003	0.002	0.318	0.091	-0.077	0.034	0.035	0.092	0.015	0.009	0.023	-0.025	-0.011	-0.000	0.105	-0.220
	25	0.019	0.023	0.002	C.CO3	0.004	-0.238	-0.223	0.199	-0.093	-0.107	-0.274	-0.040	-0.030	-0.066	0.073	6.010	-0.011	0.010	0.013
	292	-0.003	-0.000	0.000	0.000	0.002	0.027	0.035	-0.083	-0.162	-0.134	-0.033	-0.164	0.318	-0.082	0.146	0.029	-0.151	-0.062	-0.200
	2P K	-0.000	0.003	-0.001	-0-031	0.003	-0.073	0.065	0.086	-0.124	0.201	0.107	0.029	-0.043	0.199	0.099	-0.054	-0.151	-0.347	-0.043
	2 P ¥	C .00 3	0.002	0.002	0.002	0.002	-0.088	-0.099	-0.072	0.038	0.085	0.090	0.109	0.290	0.054	0.069	-0.256	-0.044	-0.105	0.220
48	15	0.003	-0.004	0.703	-0.703	0.000	0.074	-0.116	0.071	-0.064	0.050	0.079	-0.040	0.008	-0.037	-0.026	-0.002	0.016	-0.021	0.012
	25	-0.002	0.002	0.020	-0.020	0.003	-0.136	0.264	-0.174	0.166	-0.144	-0.232	0.123	-0.030	0.110	0.079	0.003	-0.049	0.044	-0.059
	292	-0.000	0.000	-0.001	0.001	0.002	0.011	-0.034	-0.014	-0.127	-0.057	0.033	0.222	0.022	0.149	0.070	0.193	0.213	0.027	0.305
	ZPX	0.001	-0.001	-0.001	0.002	-0.002	0.055	-0.041	0.055	0.041	-0.142	-0.038	0.133	-0.022	0.201	0.011	-0.006	0.020	-0.330	-0.269
	2.04	0.002	-0.002	-0.002	0.002	-0.000	0.031	-0.078	-0.044	-0.001	0.060	-0.149	0.051	-0.226	0.059	0.003	-0.224	-0.125	0.047	0.299
25	15	0.003	0.004	-0.703	-0.703	0.000	-0.074	-0.110	-0.071	-0.064	0.050	-0.079	0.040	0.008	-0.037	-0.026	0.002	0.016	0.021	-0.012
	£.	-0.002	-0.002	-0.020	-0.020	0.003	-0.130	-0.204		0.100	-0.144	0.232	-0.123	-0.030	0.110	0.079	-0.003	-0.049	-0.084	0.059
	201	-0.000	-0.000	-0.001	-0.001	0.002	-0.055	-0.041	-0.055	-0.041		-0.033	-0.222	0.022	0.149	0.070	-0.193	0.213	-0.027	-0.305
		-0.001	-0.001	0.001	-0.002	-0.000	-0.051	0.074	-0.011	-0.001	0.142	-0.038	0.333	0.022	-0.201	-0.021	-0.006	-0.020	-0.330	-0.249
	201	0.002	0.002	0.002	0.002	-0.000	0.011	0.076			0.000	0.149	-0.051	-0.226	0.059	0.003	0.224	-0.125	-0.047	-0.299
	Electronic energy + -275, 5640 au Two-electron energy + 183, 7597 au				97 au															
	Nuclea	r repulsion	 146. 13. 	59 au	Kir	netic energ	TY • 129.72	91 au												
	1	lotal energy	· -129.42	81 au		-E	T . 0.99	768												

Table V. Atomization Energies (au)

			4		A/A_B					
	SCF ^a	SCF ^b	Exptl	NEMO •	SCF⁰	SCF ^b	Exptl ^c	NEMO ^a		
B ₂ H ₆	-0.721	-0.917	-0.917	-1.022	1.0	1.0	1.0	1.0		
$\mathbf{B}_{4}\mathbf{H}_{10}$	-1.262	-1.659	-1.670	1.758ª	1.748	1.782	1,821	1.719		
B ₅ H ₉	-1.315	-1.762	-1.800	-1.896 ^d	1.827	1.893	1.963	1.852		
$B_{5}H_{11}$	-1.436	-1.894	-1.954	1.910e	1.989	2.034	2.131	1.868		

^a The reference atoms employ Clementi's best single- ζ exponents: E(B), -24.4984; E(H), -0.500.¹⁷ ^b The reference atoms employ optimized diborane exponents: $E(B_t)$, -24.4372; $E(H_t)$, -0.4892; $E(H_{Br})$, -0.4781. ^c S. R. Gunn and L. G. Green, *J. Phys. Chem.*, **65**, 2173 (1961). ^d Reference 7 (Slater exponents with H 1s = 1.20). ^e Reference 11 (partially optimized BH₃ exponents).

Tabel VI. Ionization Potentials

	SCF	Exptl⁰	NEMO
B ₄ H ₁₀ B ₂ H ₂	0.431	0.382	0.415
$\mathbf{B}_{5}\mathbf{H}_{11}$	0.401	0.379	0.403°

^a T. P. Fehlner and W. S. Koski, *J. Amer. Chem. Soc.*, **86**, 581 (1964). ^b Reference 7 (Slater exponents, H ls = 1.2). ^c Reference 11 (partially optimized BH₈ exponents).

expected, this ratio is always smaller than the experimental ratio, because of lack of exponent optimization in the calculations for the larger boron hydrides. First ionization potentials calculated from the orbital eigenvalues are compared in Table VI with those from NEMO calculations and with the experimental values.

The inconsistent agreement of these energy-related quantities with experiment emphasizes the care which must be exercised when using minimum basis set SCF wave functions in interpretations of energetics. However, schemes which allow some estimation of the correlation energy²⁰⁻²³ have been used to obtain

(21) E. Clementi, J. Chem. Phys., 38, 2248 (1963).

(22) C. Hollister and O. Sinanoğlu, J. Amer. Chem. Soc., 88, 13 (1966).

reaction energies of chemical accuracy from Hartree-Fock SCF wave functions. The Koopmans ionization potentials seem especially sensitive to changes in orbital exponents. NEMO calculations¹¹ using partially optimized BH₃ orbital exponents (B ls = 4.68, B 2s = 1.38, B 2p = 1.35, H ls = 1.20) give ionization potentials similar to those obtained from our SCF calculations, while Table VI indicates that the use of Slater exponents in NEMO calculations⁷ yields markedly different ionization potentials. This sensitivity is also evident in B₂H₆, where both Slater²⁴ and optimized⁸ basis sets have been used in SCF computations.

The accurate SCF wave functions also enable us to check some of the approximations of the NEMO theory. In Table VII we list the relevant SCF Hamil-

Table VII. Comparison of Diagonal SCF Hamiltonian Matrix Elements and NEMO α 's (au)

	F _{B 28}	$F_{\rm B\ 2p}{}^{\rm av}$		$F_{\rm H\ 1s}$
B ₂ H ₆	-1.133	-0.318	Ht	-0.473
			H_{b}	-0.566
B_4H_{10} 1B	-1.177	-0.275	$1 H_t$	-0.465
2B	-1.156	-0.247	$3H_t$	-0.491
			$5H_t$	-0.477
			$1 \mathbf{H}_{\mathbf{b}}$	-0.527
B₅H₀ 1B	-1.175	-0.277	$1H_t$	-0.418
2B	-1.201	-0.297	$2H_t$	-0.464
			$1H_b$	-0.576
$B_{5}H_{11}$ 1B	-1.192	-0.295	$1 H_t$	-0.439
2B	-1.225	-0.319	$2H_t$	-0.605
4 B	-1.153	-0.242	$3H_t$	-0.483
			$5H_t$	-0.461
			$7H_t$	-0.478
			$1H_b$	-0.619
			$2H_{b}$	-0. 599
NEMO ^a	-1.081	-0.337	H_t	-0.464
• • • • • • • • • • • • • • • • • • •			Hb	-0.593

^a Reference 7.

tonian matrix elements and the diagonal Hamiltonian elements (α 's) used by Boer, Newton, and Lipscomb.7,11 These comparisons show that the use of single values of α for all terminal or bridge hydrogens or for all borons produces serious errors in charge distributions and eigenvalues. We observe in Table VII that the BH₂ borons (B_4H_{10} , 2B; B_5H_{11} , 2B) have α 's which are higher than those for any of the other borons. We also find that apical terminal hydrogens $(B_5H_9, 1H_t; B_5H_{11}, 1H_t; \alpha_{av} = 0.428)$ may be distinguished from other terminal hydrogen (α_{av} = -0.473) by their higher values of α . Bridge hydrogen α 's are always more negative than terminal hydrogen α 's except for $2H_t$ in B_5H_{11} . This unique hydrogen assumes a value for α characteristic of a bridge hydrogen. Although this atom is designated as a normal terminal hydrogen in formal valence structures, its geometric position and participation in multicenter localized bonding⁹ make such distinctions ambiguous. Unfortunately, even within the groups of chemically similar atoms noted above there are still significant variations in α . The applicability of such a grouping is further reduced by its failure to take into account the anisotropy of the boron $2p \alpha$'s. Newton, Boer, and

(23) (a) P. E. Cade and W. M. Huo, J. Chem. Phys., 47, 614 (1967);
(b) *ibid.*, 47, 649 (1967).
(24) W. E. Peller and W. N. Limman, J. Amag. Chem. Soc. 88, 2024.

(24) W. E. Palke and W. N. Lipscomb, J. Amer. Chem. Soc., 88, 2384 (1966).

Lipscomb suggested that unreasonable charge distributions in their NEMO calculations might be due to overestimation of the boron 2s, 2p zero-overlap Hamiltonian matrix elements. The B 2s, B 2p₂ matrix element for 1B in $B_{\delta}H_{\vartheta}$ in our calculation is 0.2137, somewhat smaller than the NEMO value (0.250). Also, B 2s, B 2p elements for boron atoms bonded to two terminal hydrogens are approximately 0.06 to 0.08, slightly smaller than the 0.10 for the B 2s, B 2p₂ element in the B₂H₆ calculation which Newton, Boer, and Lipscomb used for calibration of their zero-overlap approximation factor.

Population Analysis

The Mulliken charges and significant overlap populations²⁵ for B_4H_{10} , B_5H_9 , and B_5H_{11} are given in Tables VIII and IX. We omit an atom-by-atom

Table VIII. Charge Distributions

Atom	4H ₁₀ Charge	Atom	₅H9— Charge	——В Atom	5H11 — Charge
1B 3B 1Ht 3Ht 5Ht 1Hb	$\begin{array}{c} -0.02 \\ +0.08 \\ -0.05 \\ -0.07 \\ -0.07 \\ +0.06 \end{array}$	1B 2B 1H _t 2H _t 1H _b	$\begin{array}{c} 0.00 \\ +0.06 \\ -0.09 \\ -0.04 \\ +0.01 \end{array}$	1B 2B 4B 1H _t 2H _t 3H _t 5H _t 7H _t 1H _b 2H _b	$\begin{array}{c} -0.08 \\ +0.05 \\ +0.09 \\ -0.07 \\ +0.06 \\ -0.03 \\ -0.06 \\ -0.07 \\ +0.03 \\ +0.06 \end{array}$

Table IX. Bond Overlap Populations

	Bond	Distance, Å	Overlap populations
B_4H_{10}	1B-2B	1.75	0.534
	1B-3B	1.84	0.299
	$1B-1H_t$	1.19	0.825
	$3B-3H_t$	1.19	0.819
	$3B-5H_t$	1.19	0.830
	$1B-1H_{b}$	1.33	0.4 79
	$3B-1H_b$	1.43	0.285
B₅H₀	1 B –2 B	1.66	0.531
	2B-3B	1.77	0.347
	$1B-1H_t$	1.19	0.832
	$2B-2H_{t}$	1.19	0.821
	$2B-1H_{b}$	1.35	0.388
B_5H_{11}	1 B –2 B	1.72	0.476
	1 B -4 B	1.85	0.324
	2B-3B	1.77	0.337
	2B-4B	1.72	0.414
	$1B-1H_t$	1.19	0.833
	$1B-2H_t$	1.19	0.613
	$2B-3H_{t}$	1.19	0.840
	$4B-5H_t$	1.19	0.821
	$4B-7H_t$	1.19	0.801
	$2B-1H_{b}$	1.34	0.381
	$2B-2H_{b}$	1.34	0.418
	$4B-2H_{b}$	1.32	0.330
	4B-2Ht	1.71	0.093

comparison of these results with those obtained from nonempirical molecular orbital (NEMO)^{7,11} and extended Hückel (EH)²⁶ calculations on these molecules because of the difference in basis sets employed, since

(25) R. S. Mulliken, J. Chem. Phys., 23, 1833 (1955).

(26) R. Hoffmann and W. N. Lipscomb, ibid., 37, 2872 (1962).

some wave functions which give nearly identical total electron densities give quite different Mulliken populations when decomposed in terms of different basis sets.^{8,27} However, some of the more interesting trends are noted below.

Our atomic charges, as expected, are all smaller in magnitude than those calculated by the non-selfconsistent methods.^{7,11,26} We find that for all three molecules terminal hydrogens are slightly (<0.1 e)negative, while bridge hydrogens are slightly positive. These charges agree with those calculated⁸ with the same exponents in B_2H_6 , where the terminal hydrogen had a charge of -0.07 e while the charge on bridge hydrogen was +0.01 e. The only exception found to the above rule was the unique terminal hydrogen $2H_{t}$ in $B_{5}H_{11}$. This atom is the only known example of a second terminal hydrogen bonded to a boron which is connected to more than two other boron atoms. Lipscomb² has suggested that the lack of splitting of the 1B peak by this hydrogen in the ¹¹B nmr^{28,29} implies that 2H_t is similar in character to a bridge hydrogen, as noted above. Our calculation of the charge on $2H_t$ of B_5H_{11} confirms this hypothesis.

The boron charges are quite small (<0.1 e), even smaller than the 0.13 e calculated for B_2H_6 .⁸ The apical positions in the two pentaboranes are markedly more negative than the basal positions, and borons bonded to two terminal hydrogens are found to be somewhat more positive than borons bonded to only one. It is interesting to note that Lipscomb³⁰ as early as 1956 predicted that the pentaboranes would have small charge separations and that the apical borons would be most negatively charged, by considering simplified LCAO molecular models. However, comparison of these atomic charges with the diagonal F-matrix elements (Table VII) indicates that the ω technique is not valid in its usual single linear form.

A comparison of the boron charges with those predicted by the three-center valence theory^{2,26} shows agreement in the order of the charges for B_5H_9 , and distinguishes between apical and basal boron in B_5H_{11} . These two calculations disagree in the charges predicted for the basal boron atoms of B_5H_{11} , for which the three-center charges are $q_{2B} = +0.39$, $q_{4B} = -0.06$, while $q_{2B} = +0.05$ and $q_{4B} = +0.09$ in the SCF calculations. Three-center theory predicts all boron atoms in B_4H_{10} to be neutral.

Comparison of our charge distributions with those calculated by other more approximate methods^{11,24,26,31,32} indicates good agreement with hydrogen charges (where given), but considerable disagreement in boron charges.

This disagreement among the various methods is not at all surprising in view of the fact that SCF calculations, even on B_2H_6 , show large disagreement in charge distributions between optimized Slater,8 unoptimized Slater,²⁴ and gaussian³³ basis sets. A recent

investigation²⁷ has shown that even the small changes in electron density produced by going from isotropic to anisotropic 2p orbitals in HCN produce rather large changes in the atomic charges because of modifications in the partitioning of the density. We would suggest that such small charge differences as we have found here should not be taken as an infallible guide to chemical behavior, but that they be used with caution in drawing inferences about molecular properties which may be evaluated by comparison with experiment.

Although the overlap populations are also dependent on the choice of basis set and the partitioning used, we find better agreement here with other calculations than for charges because the overlap populations are determined to a very great extent by the molecular geometry. The B-H_t values appear to be nearly independent of molecular environment, the average $B-H_t$ overlap for the three molecules being B_4H_{10} , 0.825; B_5H_9 , 0.823; and B_5H_{11} (omitting 1B-2H_t), 0.822. All bonds of this type have overlap populations within 0.02 of the average. The fluctuation in $B-H_b$ overlap populations is somewhat greater, but the average for a molecule seems to be fairly constant. The values for the average $B-H_b$ overlap populations are 0.382 for B_4H_{10} , 0.388 for B_5H_9 , and 0.376 for B_5H_{11} . As expected, the asymmetric B-H-B bridges in B_4H_{10} and the unique hydrogen $2H_t$ in B_3H_{11} showed markedly asymmetric overlap populations.

The overlap populations for the $2B-2H_{b}-4B$ bond in B_5H_{11} are quite significant. No experimental determination has yet been made of whether this bridge hydrogen lies closer to 2B or to 4B. In our calculation we had $2H_b$ very slightly (0.02 Å) closer to 4B. However, the overlap populations are 0.418 for $2B-2H_{\rm b}$ and 0.330 for $4B-2H_{\rm h}$, an asymmetry opposite in direction to the small difference in the assumed geometry. Therefore, we predict that further structural studies will show that the asymmetric bridge hydrogen in B_5H_{11} is closer to the BH group than to the BH₂ group. In B₄H₁₀, for which the B-H-B geometry is known,¹³ the bridge hydrogen is 0.2 Å closer to the B-H group, and the overlap populations calculated with the asymmetric bridge agree with this displacement $(1B-1H_b)$ = $0.479, 3B-1H_{\rm b} = 0.285$).

Boron-boron overlap populations vary over a wide range, but generally tend to confirm the valence structures shown in Figures 1-3. Borons bonded directly to each other show overlap populations higher than do borons bonded through hydrogen bridges; the difference in overlap population is generally about half of the $B-H_b$ population.

The unique hydrogen $2H_t$ in B_3H_{11} shows an abnormally small overlap population (0.613) with its bonding boron 1B. However, the difference between this value and the normal $B-H_t$ overlap population is compensated for by the unusually large nonbonded positive overlap population (0.093) between $2H_t$ and the two borons 4B and 5B. Thus we have further evidence for the remarkable role which this atom plays in the structural chemistry of boron hydrides.

If the bonds are listed in order of overlap populations, our results agree quite well with the orders calculated by NEMO, EH, and three-center theory, although the magnitudes differ considerably. There is a discrepancy in B_5H_{11} , where Boer¹¹ and Hoffmann

⁽²⁷⁾ E. Switkes, R. M. Stevens, and W. N. Lipscomb, J. Chem. Phys., 51, 5229 (1969).

⁽²⁸⁾ R. E. Williams, S. G. Gibbins, and I. Shapiro, ibid., 30, 320 (1959).

⁽²⁹⁾ R. Schaeffer, J. N. Shoolery, and R. Jones, J. Amer. Chem. Soc., 79, 4606 (1957).

⁽³⁰⁾ W. N. Lipscomb, J. Chem. Phys., 25, 38 (1956).

⁽³¹⁾ E. B. Moore, Jr., J. Amer. Chem. Soc., 85, 676 (1963).
(32) J. E. Larcher and J. W. Linnett, Theor. Chim. Acta, 12, 127

⁽¹⁹⁶⁸⁾ (33) L. Burnelle and J. J. Kaufman, J. Chem. Phys., 43, 3510 (1965).



Figure 4. Total electron density (electrons/au³) in the 1B-2B-3B plane of B_4H_{10} .



Figure 5. Total electron density (electrons/au³) in the 1B-2B-3B plane of B_5H_9 .

and Lipscomb²⁶ find the 1B-4B overlap population to be nearly as great as that for 1B-2B, while we find the former to be the lowest B-B population in the molecule.

Finally, we find no evidence for the large negative (-0.62) 1B-2B overlap populations in B₅H₉ calculated by Larcher and Linnett.³² Thus the necessity for invoking ionic bonding between essentially neutral boron atoms in order to explain the molecular stability³² does not arise in our calculation.

Perhaps a more accurate picture of bonding in these boron hydrides is provided by the total density maps in Figures 4–8. These maps tend to confirm the conclusions drawn from the population analysis, but unlike the total charges and overlap populations, the point density is invariant to a transformation within the basis set. In Figure 4 we show the density in the plane determined by the atoms 1B, 2B, and 3B in B_4H_{10} . The strong bonding between 1B and 2B is in striking contrast



Figure 6. Total electron density (electrons/au³) in $1H_t-1B-2H_t$ plane of B_sH_{11} .



Figure 7. Total electron densities (electrons/au³) of the boronboron bonds in B_8H_{11} : (a) 1B-2B-3B plane, (b) 1B-2B-4B plane.



Figure 8. Total electron densities (electrons/au³) of the bridge hydrogen bonds in B_5H_{11} : (a) $3B-3H_b-5B$ plane, (b) $2B-1H_b-3B$ plane.

to the much lower densities in the 1B-3B internuclear region. Although the bridge hydrogens $1H_b$ and $2H_b$ are not directly in the 1B-2B-3B plane, the shadows³⁴ of the hydrogen bridge bonds can be seen in Figure 4. In Figure 5 the total electron density in the 1B-2B-3B plane of B_5H_9 is shown along with the shadow of the three-center bridge bond involving $1H_b$. This map clearly shows bonds between apical and basal-plane borons, and B-H_b-B bonding involving borons in the

(34) When a substantial electron density is present from a bond involving an atom not quite in the plane selected for the section, we refer to this density as the shadow of that bond.



Figure 9. Difference density (molecular – spherical atoms; electrons/au³) in the three-center 1B-2B-4B bond in B_5H_{11} : positive contours (-) +0.003 electron/au³, negative contours (--) -0.003 electron/au³.

fourfold positions. The electron density in the 2B-3Binternuclear region is considerably lower. Some insight into the rather unique properties of $2H_t$ in B_5H_{11} may be gained from Figure 6, which shows the total density in the $1H_t-1B-2H_t$ plane of B_5H_{11} . Although equal bond distances were assumed for the $1B-1H_t$ and $1B-2H_t$ bonds, and these two hydrogens were assigned the same orbital exponent, the difference in the bonding densities is striking. Comparison with Figure 8 indicates that the density in the 1B-2H_t bond is intermediate between that in the 1B-1H_t terminal bond and those in the 2B-1H_b-3B and 2B-2H_b-4B bridge hydrogen bonds. In Figure 7 we show the total densities in the two nonequivalent three-boron planes in B_5H_{11} . The bonding between the apical and basal borons in the symmetric 1B-2B-3B plane of B_5H_{11} , as shown in Figure 7a, is similar to that found in B_5H_9 . Electron density in the asymmetric 1B-2B-4B bonding plane is shown in Figure 7b. In this plane the bonding density originating at atom 4B is not directed exactly toward any other atom. The relevance of this observation to three-center boron bonding is discussed more fully in the following paper.9 In Figure 8a we exhibit the asymmetric nature of the 3B-3H-5B bridge hydrogen bond. As was noted in the overlap population analysis, bonding of a bridge hydrogen to a B-H_t boron appears to be stronger than that of a bridge hydrogen to $B(H_t)_2$. Figure 8b shows symmetric three-center hydrogen bridge bonding in the $2B-1H_b-3B$ plane.

Further insight into the nature of bonding may be obtained by considering difference electron densities. In Figure 9 we display a difference density map for the asymmetric three-boron plane in B_5H_{11} . This map was constructed using SCF atomic wave functions from a calculation which employed the same basis orbitals as used for the boron and hydrogen atoms in our molecular calculations.¹⁹ We have chosen to subtract these spherical atomic densities rather than valencestate atomic densities³⁵ from our molecular density. In this manner we can see the effects of valence-state promotion and quantum mechanical interference on the bonding density. Figure 9 illustrates the accumulation of promotion and interference density in the central 1B-2B-4B bond in B_5H_{11} . It is to be remembered, however, that mechanisms other than valence-state promotion and interference (e.g., electrostatic interactions, orbital contractions)¹⁸ can be responsible for bonding. Interpretation of these difference densities must also include the realization that in polyatomic molecules several bonds may compete for the available electron density on an atom, and thus a negative difference density can exist along a bonding direction where the total density exhibits a relative maximum.

Dipole Moments

Although the molecular dipole moment is not a unique measure of the electron density, dipole moments (Table X) provide a reliable test of the adequacy of our

Table X. Dipole Moments (D)

	$\mu_{classical}$	$\mu_{\rm atom}$	$\mu_{\texttt{bond}}$	#total	μ_{exptl}
B ₄ H ₁₀ SCF ^a	0.76	0.38	-0.14	1.00	0.56ª
$B_{5}H_{9}$ SCF ^a	1.54 -1.54	-2.44	0.42	2.69 	-2.13
NEMO ^b B.H., SCF ^a	-5.16	-1.86	-1.46	-8.48	
NEMO°	1.61	1.47	0.57	3.98	

^a Present work. ^b Reference 7. ^o Reference 11. ^d Reference 36. ^e Reference 37.

wave functions, since the total moments are independent of basis-set partitioning and can be directly measured experimentally. Atomic, bond, and classical (Mulliken point charge) contributions to the dipole moments were calculated using the origin-invariant partitioning method of Ruedenberg.¹⁸ The results are shown in Table XI. Our values for the two molecules, B_4H_{10} and B_5H_9 , whose dipole moments have been measured^{36, 37} are somewhat better than those calculated by NEMO,⁷ but are still nearly twice the experimental value. This discrepancy can be attributed to our use of a partially optimized minimum basis set³⁸ and will probably also occur in B_5H_{11} , the dipole moment of which has not yet been measured.

The NEMO values for the various contributions to the dipole moment are also included in Table X, although this partitioning is somewhat dependent on the basis set. Extended Hückel values for dipole moments are probably unreliable, as evidenced by a number of recent studies³⁹ of this method and the fact that the two different sets of empirical parameters used by Hoffmann and Lipscomb²⁶ gave values for $B_{\delta}H_{9}$ which differed by a factor of 5.5.

The dipoles predicted by consideration of all threecenter valence structures²⁶ are 0, 4.07, and 2.36 D for

- (37) H. J. Hrostowski, R. J. Meyers, and G. C. Pimentel, *ibid.*, 20, 518 (1952).
- (38) B. J. Ransil, Rev. Mod. Phys., 32, 239 (1960).
- (39) See, e.g., A. Pullman, Int. J. Quantum Chem., 25, 187 (1968).

^{(35) (}a) R. F. W. Bader, W. H. Henneker, and P. E. Cade, J. Chem. Phys., 46, 3341 (1967); (b) R. F. W. Bader, I. Keaveny, and P. E. Cade, *ibid.*, 47, 3381 (1967).

⁽³⁶⁾ J. R. Weaver, C. W. Hertsch, and R. W. Parry, *ibid.*, 30, 1075 (1959).

Table XI. Atomic and Bond Moments (D)

	B ₄ H ₁₀			B₅H	I9	∃ ,, ≣ ,,,, , , , , , , , , , , , , , , , , ,		B5H11	
	Z	Total		Ζ	Total		У	Z	Total
$\begin{array}{c} 1B\\ 2B\\ 1B-2B\\ 1B-3B\\ 3B-3H_t\\ 3B-5H_t\\ 1B-1H_b\\ 3B-1H_b \end{array}$	$\begin{array}{c} 0.38 \\ -0.20 \\ 0.20 \\ 0.02 \\ -1.32 \\ 0.74 \\ -0.49 \\ 0.07 \end{array}$	0.38 0.50 0.20 0.03 1.32 1.34 0.86 0.52	1B 2B 1B-2B 2B-3B 1B-1H _t 2B-2H _t 2B-1H _b	$ \begin{array}{r} -0.42 \\ -0.50 \\ -0.29 \\ -0.05 \\ -1.23 \\ -0.35 \\ 0.55 \\ \end{array} $	0.42 0.55 0.44 0.16 1.23 1.28 0.71	1B 2B 4B 1B-2B 1B-4B 2B-3B 2B-4B 1B-1H _t 1B-2H _t 2B-3H _t 4B-5H _t 4B-5H _t 4B-7H _t 2B-2H _b 4B-2H _b 4B-2H _b	$\begin{array}{c} -0.01\\ 0.20\\ -0.34\\ 0.04\\ 0.06\\ 0.03\\ -0.02\\ 0.10\\ -1.04\\ 1.00\\ -0.07\\ -0.97\\ 0.21\\ -0.29\\ 0.45\\ 0.05\end{array}$	$\begin{array}{c} -0.34\\ -0.43\\ 0.12\\ -0.16\\ -0.10\\ 0.00\\ -0.13\\ -1.31\\ 0.38\\ -0.51\\ -0.75\\ 0.85\\ 0.54\\ 0.59\\ 0.47\\ 0.11\\ \end{array}$	$\begin{array}{c} 0.34\\ 0.52\\ 0.41\\ 0.23\\ 0.16\\ 0.03\\ 0.18\\ 1.31\\ 1.11\\ 1.28\\ 1.32\\ 1.32\\ 0.72\\ 0.78\\ 0.65\\ 0.20\end{array}$

 B_4H_{10} , B_5H_9 , and B_5H_{11} , respectively. Agreement with our results is fair. Our values for the pentaboranes also fall well below the three-center single valence structure upper limits of 5.23 D for B_5H_9 and 4.75 D for B_5H_{11} calculated by Eberhardt, Crawford, and Lipscomb.⁴⁰ The prediction by these authors that such negligible dipole moment as exists in B_4H_{10} will be due to B-H bond contribution rather than formal charge separation is not borne out by our results. In fact, though the individual B-H bond moments are quite large (0.50–1.25 D vs. 1.00 D for the dipole moment), they tend to cancel each other, and the net bond moment actually opposes the total dipole moment.

Values for atomic and bond moments in the three molecules are given in Table XI. These components are generally smaller than in the NEMO calculations⁷ on B_4H_{10} and B_5H_9 , which are the only other calculations for which such an analysis was available. Boron atomic moments all lie between 0.35 and 0.55 D, while B-B bond moments are much smaller-less than 0.25 D, except for the anomalously large value of 0.43 D for 1B-2B in B_5H_9 . Like overlap populations, B-H_t bond moments are remarkably independent of molecular environment and are all about 1.3 D. Bridge B-H moments are somewhat smaller and much more variable. The $1B-2H_t$ "pseudobridge" in $B_{\delta}H_{11}$ is again exceptional with a moment about 0.2 D too low for a B-H_t bond being compensated for by a $4B-2H_t$ moment of approximately the same magnitude, far too large for a normal nonbonded B-H interaction. We note that both our SCF atomic and bond moments show far more constancy from molecule to molecule and from position to position within a molecule than do their NEMO counterparts.

In all three molecules the net bond moment is small and opposite in direction to the total dipole moment. This effect is due completely to the fact, noted by Boer, Newton, and Lipscomb,⁷ that bridge B-H bonds make large contributions in opposition to the net molecular moment. The (negative) bridge contributions to the three dipole moments are 1.7, 4.4, and 3.3 D for B_4H_{10} , B_5H_9 , and B_5H_{11} , respectively.

Although our total dipole moments for B_4H_{10} and B_5H_9 are still nearly twice the experimental values, we feel that their order is probably correct and that one

(40) W. H. Eberhardt, B. Crawford, and W. N. Lipscomb, J. Chem. Phys., 22, 989 (1954).

may reliably predict that the dipole moment of B_5H_{11} will be found to be between those of B_4H_{10} and B_5H_9 , probably somewhat closer to the latter.

Magnetic Properties

A comparison of ¹¹B nmr shifts vs. net Mulliken charges²⁵ (Table XII) shows the expected correlation

Table XII. ¹¹B Nmr Shifts vs. Net Mulliken Charges

		σ, ^{a,b} ppm	q
B_4H_{10}	1 B	40.0, 41.8	-0.02
	3 B	6.5, 6.9	0.08
B₅H₃	1 B	51.8	0.00
	2B	12.7	0.06
B_5H_{11}	1 B	53.5	-0.08
	2B	31.7	0.05
	4 B	2.3	0.09

^a Relative to boron trifluoride etherate. ^b Reference 43.

between increasing negative charge and increasing magnetic shielding. The magnitude of the change, however, is too great to be explained by the variation in the Lamb⁴¹ diamagnetic term alone, since the addition of one 2p electron to the boron atom gives a calculated increase in the diamagnetic term of only 13.1 ppm. Changes of the magnitude observed must be largely the result of changes in the paramagnetic or high-frequency terms. Optimization of the boron 2p exponents may be required for the accurate evaluation of these terms.⁴² Three of the borons given are more shielded than is the borohydride ion (σ_{NaBH} = 38.7 ppm), for which the one-center paramagnetic term (in the minimum basis set approximation) is zero as a result of the equivalence of the p-orbital components. Thus the explanation of these high-field shifts must be contained in the two-center or "neighbor anisotropy" contributions to the paramagnetic term.

In all of our SCF calculations the bridge hydrogens are positive. It is therefore doubtful whether the experimental^{43,44} high-field shift of the bridge hy-

(43) R. Schaeffer, "Progress in Boron Chemistry," Vol. 1, H. Steinberg and A. L. McCloskey, Ed., Macmillan and Co., New York, N. Y., 1964, p 417.

⁽⁴¹⁾ W. E. Lamb, Phys. Rev., 60, 817 (1941).

⁽⁴²⁾ M. Karplus and J. A. Pople, J. Chem. Phys., 38, 2803 (1963).
(43) R. Schaeffer, "Progress in Boron Chemistry," Vol. 1, H. Stein-

⁽⁴⁴⁾ G. Eaton and W. N. Lipscomb, "NMR Studies of Boron Hydrides and Related Compounds," W. A. Benjamin, Inc., New York, N. Y., 1969.

drogens can be explained without considering twocenter paramagnetic contributions to the chemical shift. The fact that hydrogens bonded to high-field borons (generally more negative) resonate at higher field and are more positively charged (less shielded diamagnetically) is another indication of the importance of paramagnetic terms. The paramagnetic contributions to the proton shielding may be approximated as a "neighbor anisotropy"⁴⁵ effect of the boron atoms if accurate values for susceptibility components can be calculated for these borons.

Reactivity

Efforts to correlate known boron hydride reactions with the results of our calculations are severely limited by a scarcity of experimental data and of clear-cut interpretations of reaction pathways. We shall, however, briefly discuss a few substitution reactions with reference to three of the more directly calculable indices of reactivity-atomic charges, frontier orbital populations, and free valences. Two of the authors (I. R. E. and J. A. T.) are now studying the application of more sophisticated methods to the calculation of boron hydride reactivities.

Two frequently applied criteria for predicting reactivity in ionic reactions are the atomic charges and the populations of the highest filled and lowest vacant molecular orbitals. In the first approximation one expects that nucleophilic substitution will take place most easily at the boron atom with the greatest positive (or lowest negative) charge or at the boron with the greatest population in the lowest vacant orbital. Similarly, electrophilic substitution is expected to occur at the site of greatest negative charge and greatest highest filled MO population. Our calculations of the atomic charge and frontier orbital criteria agree in predicting the order of ionic reactivities at the various atomic sites, with the exception of 2B and 4B in B_5H_{11} . The predicted order of reactivity for nucleophilic substitution is 3B > 1B in B_4H_{10} , 2B > 1B in B_5H_9 , and 4B > 2B > 1B (charge) or 2B > 4B > 1B (lowest vacant MO) in B_5H_{11} . For electrophilic substitution one should find the reverse ordering of reactivity.

The only one of the three molecules for which electrophilic substitution has been definitely observed is B_5H_9 . Gaines and Martens⁴⁶ found that substitution took place at 1B when B_5H_9 was chlorinated using AlCl₃ as the catalyst. Further evidence for electrophilic substitution at 1B is provided by the AlCl₃catalyzed exchange of D with H in B₅H₉.⁴⁷ Also pentaborane(9) reacts with I₂ only at 1B,⁴⁸ and reactions with iodine by nonionic mechanisms are exceedingly rare. Finally, Friedel-Crafts ethylation of B_3H_9 occurs almost exclusively at the apical boron position.⁴⁹

The concept of free valence⁵⁰ has been used to great advantage in the study of reactivities of conjugated systems. One predicts that the most reactive atom (i) in free-radical substitutions will be the one for which

(47) T. P. Onak and R. E. Williams, ibid., 1, 106 (1962).

(50) C. A. Coulson, Discuss. Faraday Soc., 2, 9 (1947).

 $\sum_{i} p_{ij}$ is least (where the p_{ij} are the bond orders between atom i and its nearest neighbors j). A similar calculation using as our index

$$\sum_{\substack{j\neq i\\P_{ij}>0}} P_{ij}$$

where the P_{ij} 's are the Mulliken overlap populations, gives the following predicted order for free radical substitutions: 1B > 3B in B_4H_{10} , 2B > 1B in B_5H_9 , and 4B > 2B > 1B in B_5H_{11} .

Dobson and Schaeffer⁵¹ found that B₄H₁₀ reacts with bromine (uncatalyzed) to give $3-B_4H_9Br$. This result contradicts our prediction that 1B is more reactive, if the reaction does indeed proceed by a free-radical mechanism. However, the experiment is by no means unambiguous, and nucleophilic substitution remains a possibility. On the other hand, the displacement of bridge hydrogens toward the BH groups may leave the 3-boron sterically more available for formation of an activated complex. Gaines and Martens⁴⁶ also found, if they omitted the AlCl₃ when chlorinating B_5H_9 , that the product was the 2-substituted pentaborane. This result suggests a free-radical pathway. Also, Burg⁴⁸ found mainly 2-substituted ClB₅H₈ and FB₅H₈ in uncatalyzed gas-phase flow reactions. The evidence, then, seems to indicate that $B_{\delta}H_{\vartheta}$ reacts by free-radical mechanisms at 2B as predicted.

Analysis of the product of the gas-phase reaction of B_5H_{11} with a mixture of mono- and dimethyl diboranes⁵² indicates that a proton is replaced by a methyl group at 4B. Although the mechanism is by no means clear, a free-radical reaction seems fairly likely, in agreement with our prediction.

Thus simple reactivity indices do correlate fairly well the observed boron hydride reactivities. Great caution must be observed here, however, both because of the uncertainties in interpretation of the experiments and because of the crudeness of such measures of reactivity as atomic charges, which can depend on the choice of basis set. It is hoped that these and our forthcoming reactivity studies will inspire a more definitive experimental study of the reactions of the boron hydrides.

Finally, as noted above, other factors may dominate the reaction pathway. For examples we include steric factors in the formation of an activated complex; a succession of transformations such that the initial ground state of the molecule loses its effect in favor of an intermediate in the reaction pathway; differences in coordination number, when present; and solvent effects, especially when adducts of solvent molecules to electron-deficient species may be intermediates. Nevertheless, we hope that some simplified features of reactivity and of transition states can emerge at the SCF level, and we note that some success has already been obtained in reactivity studies^{53,54} of the polyhedral carboranes at a lower level of approximation.

Acknowledgment. Three of the authors (E. S., I. R. E., J. A. T.) are indebted to the National Science Foundation for predoctoral fellowships. We also are grateful to the Office of Naval Research for support of this research.

- (51) J. Dobson and R. Schaeffer, Inorg. Chem., 4, 593 (1965).
- (52) C. A. Lutz and D. M. Ritter, *Can. J. Chem.*, 41, 1344 (1963).
 (53) J. A. Potenza and W. N. Lipscomb, *Inorg. Chem.*, 5, 1301 (1966).
- (54) H. A. Beall and W. N. Lipscomb, ibid., 6, 874 (1967).

⁽⁴⁵⁾ J. A. Pople, J. Chem. Phys., 37, 53 (1962).

⁽⁴⁶⁾ D. F. Gaines and J. A. Martens, Inorg. Chem., 7, 704 (1968).

 ⁽⁴⁸⁾ A. B. Burg, J. Amer. Chem. Soc., 90, 1407 (1968).
 (49) N. J. Blay, I. Dunstan, and R. L. Williams, J. Chem. Soc., 430

⁽¹⁹⁶⁰⁾